



फॅक्स : ००९१-०२३१-२६९५३३ व २६९२३३३. Email bos@unishivaji.ac.in

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| 1. प्र. अधिष्ठाता, विज्ञान व तंत्रज्ञान विद्याशाखा | } | यांना माहीतीसाठी |
| 2. पीजीबीयुटीआर विभाग | | |
| 3. परीक्षक नियुक्ती विभाग | } | यांना माहीतीसाठी व पुढील योग्य त्या कार्यवाहीसाठी |
| 4. संलग्नता विभाग | | |
| 5. बी.एससी. विभाग | | |

NEW/REVISED SYLLABUS FOR M. Phil. / Ph.D. Course Work

Paper: III

Title of Paper: Theory of Fractional Dynamic Systems

Unit I: A Short History and Some Related Functions, The R-L Fractional Integrals and Derivatives, The Grunwald-Letnikov Derivative, The Caputo Derivative, The Mean Value Theorem, Dini Derivatives and Comparison Theorems, The Volterra fractional integral inequalities, Fractional Differential inequalities Local Existence and Extremal Solutions, Existence, Uniqueness and Continuous Dependence. **15 Lectures**

Unit II: Approximate Solutions and Global Existence, Linear Fractional Differential Equations, Finite Systems of Differential Inequalities, Existence of an Euler Solution, Caputo's Fractional Differential Equation, Theoretical Approximations-Theoretical and Constructive Existence Result, Generalized Monotone Iterative Technique, Monotone Method for PBVP, Generalized Monotone Iterative Technique- PBVP. **15 Lectures**

Unit III: Quasilinearization, Generalized Quasilinearization, Stability Criteria, Proximal Normal and Flow Invariance, Relation Between Fractional and Ordinary DEs, Lyapunov Theory -Basic Comparison Result, Stability Criteria, Stability Concepts in Terms of Two Measures, Stability Criteria in Terms of Two Measures, Boundedness and Lagrange Stability. **15 Lectures**

Unit IV: Several Lyapunov Functions, Multi-Order Fractional Differential Systems, Stability of Multi-Order Systems via ODEs, Fractional Functional DEs, Fractional DEs Involving Causal Operators, and Fractional DEs in a Banach space, Nonlocal Boundary Value Problems, BVP for Fractional Differential Inclusions, Almost Automorphic Solutions of Evolution Equations. **15 Lectures**

Recommended Book(s):

1. V. Lakshmikantham, S. Leela and J. Vasundhara Devi, Theory of Fractional Dynamic Systems, Cambridge Scientific Publishers, UK, 2009.

Reference Books:

1. Igor Podlubny, Fractional differential equations. San Diego: Academic Press; 1999.
2. A. Kilbas, H.M. Srivastava, J.J. Trujillo, Theory and Applications of Fractional Differential Equations, Elsevier, Amsterdam, 2006.
3. Kai Diethelm, The Analysis of Fractional Differential Equations, Springer, 2010.
4. L. Debnath, D. Bhatt, Integral Transforms and Their Applications, CRC Press, 2010.

NEW/REVISED SYLLABUS FOR M. Phil. / Ph.D. Course Work

Paper: III

Title of Paper: Differential and Integral Inequalities

Unit I: Existence and continuation of solutions, Scalar differential inequalities, Maximal and minimal solutions, Comparison theorems, Finite systems of differential inequalities, Minimax solutions, Integral inequalities reducible to differential inequalities, Differential inequalities in the sense of Caratheodory **15 Lectures**

Unit II: Global existence, Uniqueness, convergence of successive approximations, Chaplygin's method, Dependence on initial conditions and parameters, Variation of constants, Upper and lower bounds, Componentwise bounds, Asymptotic equilibrium, Asymptotic equivalence. Stability criteria, Asymptotic behavior **15 Lectures**

Unit III: The inequalities of Gronwall and Bellman, Some generalizations of the Gronwall-Bellman inequality, Volterra-type integral inequalities, The inequalities of Gamidov and Rodrigues, Simultaneous inequalities, Pachpatte's inequalities, Integro-differential inequalities, Applications-Second order integro-differential equations, Perturbation of Volterra integral equations, Higher order integro-differential equations **15 Lectures**

Unit IV: Nonlinear integral inequalities-Inequalities involving comparison, The inequalities of Bihari and Langenhop, Generalizations of Gronwall- Bellman- Bihari inequalities, Inequalities with Volterra-type kernels, Inequalities with nonlinearities in the integral, Pachpatte's inequalities I, Pachpatte's inequalities II, Integro-differential inequalities, Applications-Second order nonlinear differential equations, Perturbed integro-differential equations **15 Lectures**

Recommended Book(s):

1. V. Lakshmikantham, S. Leela, Differential and integral inequalities -Theory and applications, *Vol-I, Accademic Press, New York London, 1969.*
2. B. G. Pachpatte, Inequalities for differential and integral equations, *Accademic Press, London, 1998.*

Reference Books:

1. E. A. Coddington and N. Levinson, Theory of Ordinary Differential Equations, Tata McGraw-Hill, 1955.
2. B. G. Pachpatte, Integral And Finite Difference Inequalities and Applications, North-Holland Mathematics Studies 205, 2006
3. M. Hirsch, S. Smale and R. L. Devaney, Differential equations, dynamical systems and an introduction to chaos, Elsevier Academic Press, USA, 2004.
4. S. G. Deo, V. Lakshmikantham, V. Raghvendra, Textbook of Ordinary Differential Equations, Tata McGraw-Hill, 1997.

NEW/REVISED SYLLABUS FOR M. Phil. / Ph.D. Course Work

Paper: III

Title of Paper: Delay Differential Equations

Unit I: Introduction, DDE with Single Constant Delay, DDE with Discrete Delays, DDE with Distributed Delay, DDE with State-Dependent Delay, DDE with Time-Dependent Delay, Constructing the Solution for DDEs with Single Constant Delay, Linear Delay Differential Equation, Numerical Simulation of DDEs, Nonlinear Delay Differential Equations, Salient Features of Chaotic Time-Delay Systems **15 Lectures**

Unit II: Linear Stability Analysis, A Geometric Approach to Study Stability, A General Approach to Determine Linear Stability of Equilibrium Points **15 Lectures**

Unit III: Bifurcation and Chaos in Time-Delayed Piecewise Linear Dynamical System: Simple Scalar First Order Piecewise Linear DDE, Numerical Study of the Single Scalar Piecewise Linear Time-Delay System, Stability Analysis and Chaotic Dynamics of Coupled DDEs **15 Lectures**

Unit IV: A Few Other Interesting Chaotic Delay Differential Equations: The Mackey-Glass System, Ikeda Time-Delay System, Scalar Time-Delay System with Polynomial Nonlinearity, Scalar Time-Delay System with Other Piecewise Linear Nonlinearities, Time-Delayed Chua's Circuit, Complete Synchronization in Coupled Time-Delay Systems **15 Lectures**

Recommended Book(s):

1. M. Lakshmanan, D.V. Senthilkumar, Dynamics of Nonlinear Time-Delay Systems, Springer-Verlag Berlin Heidelberg 2010.

Reference Books:

1. Hale, Jack K., Theory of functional differential equations, Springer-Verlag Berlin Heidelberg 1928
2. Hal Smith, An Introduction to Delay Differential Equations with Sciences Applications to the Life, Springer New York, 2011.